

Original code written November 2015 by David Moore
Slight updates and formatting changes done in July 2024.

Code for generating the metric

Code I wrote for generating the metric for a Schwarzschild black hole in “Cartesian” coordinates,

```

In[1]:= coords = {t, x, y, z};
sq[v_] := v.v;
m = 1;
metric = -(1 - m / Sqrt[x^2 + y^2 + z^2]) Dt[t]^2 +
(1 - m / Sqrt[x^2 + y^2 + z^2])^(-1)  $\left( \frac{2 x Dt[x] + 2 y Dt[y] + 2 z Dt[z]}{2 \sqrt{x^2 + y^2 + z^2}} \right)^2 + sq[\{Dt[x], Dt[y], Dt[z]\} -$ 
{x, y, z}.{Dt[x], Dt[y], Dt[z]} / Sqrt[x^2 + y^2 + z^2]^2 {x, y, z}] // FullSimplify;
gfunc[list_] := Times @@ (Dt[t], Dt[x], Dt[y], Dt[z])^(list - 1);
subst = Flatten[MapIndexed[(If[gfunc[#2] != 1, gfunc[#2], foo] → #1) &,
FullSimplify[CoefficientList[metric, {Dt[t], Dt[x], Dt[y], Dt[z]}], {4}]];

Print["Finding metric"];
metricmatrix = MapIndexed[If[#2[[1]] == #2[[2]], #1, #1 / 2] &, FullSimplify[
Outer[Times, {Dt[t], Dt[x], Dt[y], Dt[z]}, {Dt[t], Dt[x], Dt[y], Dt[z]}] /. subst], {2}];
Print["Finding metric inverse"];
metricmatrixUp = FullSimplify[Inverse[metricmatrix]];

g[μ_, ν_] := metricmatrix[[μ, ν]];
gcomma[μ_, ν_, κ_] := D[g[μ, ν], coords[[κ]];
gUp[μ_, ν_] := metricmatrixUp[[μ, ν]];
Γ[i_, j_, k_] :=
1 / 2 Sum[gUp[i, l] (gcomma[l, j, k] + gcomma[l, k, j] - gcomma[j, k, l]), {l, 1, 4}];
Print["Finding equations of motion"];
eqns = Table[Dt[Dt[coords[[i]]] ==
-Sum[Dt[coords[[a]] × Dt[coords[[b]] × Γ[i, a, b] /. m → 1, {a, 1, 4}, {b, 1, 4}], {i, 1, 4}];
Print["Simplifying equations of motion"];
eqns = Simplify[eqns];

Finding metric
Finding metric inverse
Finding equations of motion
Simplifying equations of motion

```

```
In[19]:= metricmatrix // MatrixForm
```

```
Out[19]//MatrixForm=
```

$$\begin{pmatrix} -1 + \frac{1}{\sqrt{x^2+y^2+z^2}} & 0 & 0 & 0 \\ 0 & \frac{x^2 + \frac{(y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})}{\sqrt{x^2+y^2+z^2}}}{x^2+y^2+z^2 - \sqrt{x^2+y^2+z^2}} & \frac{xy}{(x^2+y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})} & \frac{xz}{(x^2+y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})} \\ 0 & \frac{xy}{(x^2+y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})} & 1 + \frac{y^2(x^2+y^2+z^2 + \sqrt{x^2+y^2+z^2})}{(-1+x^2+y^2+z^2)(x^2+y^2+z^2)^{3/2}} & \frac{yz}{(x^2+y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})} \\ 0 & \frac{xz}{(x^2+y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})} & \frac{yz}{(x^2+y^2+z^2)(-1+\sqrt{x^2+y^2+z^2})} & \frac{x^2+y^2 - \sqrt{x^2+y^2+z^2} + z^2 \left(1 + \frac{1}{\sqrt{x^2+y^2+z^2}}\right)}{x^2+y^2+z^2 - \sqrt{x^2+y^2+z^2}} \end{pmatrix}$$

```
In[20]:= metricmatrixUp // MatrixForm
```

```
Out[20]//MatrixForm=
```

$$\begin{pmatrix} \frac{1}{-1 + \frac{1}{\sqrt{x^2+y^2+z^2}}} & 0 & 0 & 0 \\ 0 & 1 - \frac{x^2}{(x^2+y^2+z^2)^{3/2}} & -\frac{xy}{(x^2+y^2+z^2)^{3/2}} & -\frac{xz}{(x^2+y^2+z^2)^{3/2}} \\ 0 & -\frac{xy}{(x^2+y^2+z^2)^{3/2}} & 1 - \frac{y^2}{(x^2+y^2+z^2)^{3/2}} & -\frac{yz}{(x^2+y^2+z^2)^{3/2}} \\ 0 & -\frac{xz}{(x^2+y^2+z^2)^{3/2}} & -\frac{yz}{(x^2+y^2+z^2)^{3/2}} & 1 - \frac{z^2}{(x^2+y^2+z^2)^{3/2}} \end{pmatrix}$$

Code for plotting a geodesic to test things

```
In[21]:= positiveTprime =
```

```

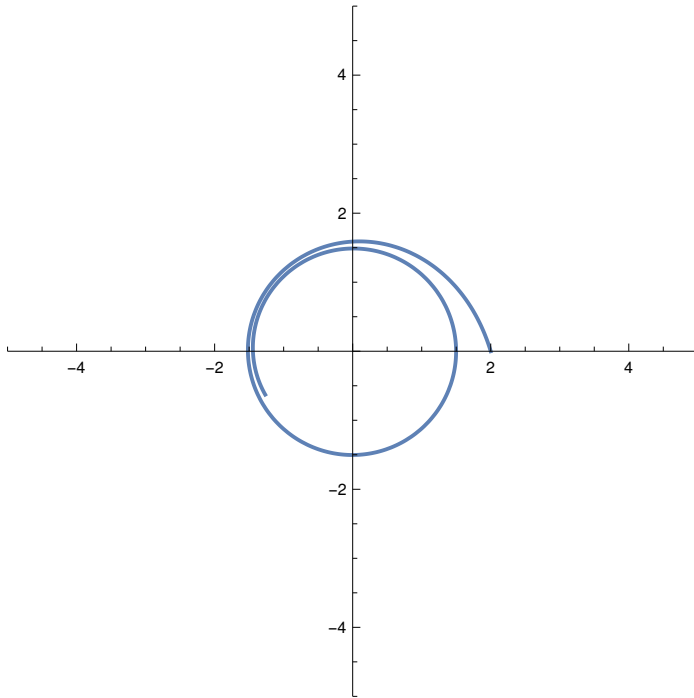
Simplify[dt0 /. Solve[{dt0, dx0, dy0, dz0}.metricmatrix.{dt0, dx0, dy0, dz0} == 0, dt0][[2]];
eqns2 = eqns /. {Dt[Dt[t]] -> t'[t], Dt[t] -> t'[t], t -> t[r],
Dt[Dt[x]] -> x'[r], Dt[x] -> x'[r], x -> x[r],
Dt[Dt[y]] -> y'[r], Dt[y] -> y'[r], y -> y[r],
Dt[Dt[z]] -> z'[r], Dt[z] -> z'[r], z -> z[r]};
plotGeodesic[x0v_, y0v_, dx0v_, dy0v_, options : OptionsPattern[]] :=
Module[{tmp, incondsub, incond, nsoln},

incondsub = {t0 -> 0., x0 -> x0v, y0 -> y0v, z0 -> 0, dx0 -> dx0v, dy0 -> dy0v, dz0 -> 0};
incond = {t[0] == t0, x[0] == x0, y[0] == y0, z[0] == z0, x'[0] == dx0, y'[0] == dy0, z'[0] == dz0,
t'[0] == Re@(positiveTprime /. {x -> x0, t -> t0, y -> y0, z -> z0})} /. incondsub;
nsoln = First@NDSolve[Join[eqns2, incond,
{WhenEvent[x[r]^2 + y[r]^2 + z[r]^2 < 2.0, "StopIntegration"]}], {t, x, y, z}, {r, 0, 100.}
];
min = (t /. nsoln)[[1, 1]];
max = (t /. nsoln)[[1, 2]];
ParametricPlot[{x[r], y[r]} /. nsoln, {r, min, max},
PlotRange -> 5, Evaluate[FilterRules[options, Options[Plot]]]]
]

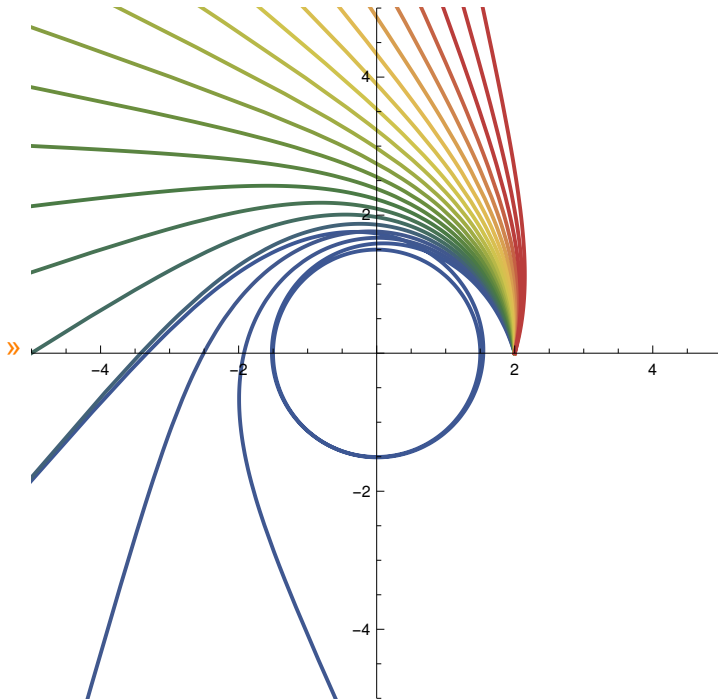
```

```
In[24]:= plotGeodesic[2, 0, -0.3043, 1]
```

```
Out[24]=
```



```
In[31]:= SetDirectory[NotebookDirectory[]];
Export["rays.png", Echo@Show[Table[plotGeodesic[2, 0, -0.30429 + i,
1, PlotStyle -> ColorData["DarkRainbow"][i / 0.6]], {i, 0, 0.6, 0.6 / 20}]]]
```



Out[32]=

rays.png

Generating the C code for integration

```
In[26]:= FullForm[Element[#, Reals] & /@ {x, y, z, t, dx, dy, dz, dt}]
```

Out[26]//FullForm=

```
List[Element[x, Reals], Element[y, Reals], Element[z, Reals], Element[t, Reals],
Element[dx, Reals], Element[dy, Reals], Element[dz, Reals], Element[dt, Reals]]
```

In[27]:= equationsSimplified =

```
FullSimplify[ddt, ddx, ddy, ddz] /. Solve[eqns /. {Dt[Dt[t]] -> ddt, Dt[t] -> dt, t -> t,
Dt[Dt[x]] -> ddx, Dt[x] -> dx, x -> x,
Dt[Dt[y]] -> ddy, Dt[y] -> dy, y -> y,
Dt[Dt[z]] -> ddz, Dt[z] -> dz, z -> z}, {ddt, ddx, ddy, ddz}][[1]],
Assumptions -> {Element[x, Reals], Element[y, Reals], Element[z, Reals], Element[t, Reals],
Element[dx, Reals], Element[dy, Reals], Element[dz, Reals], Element[dt, Reals]}
```

Out[27]=

$$\left\{ -\frac{dt(dx x + dy y + dz z)}{(x^2 + y^2 + z^2)(-1 + \sqrt{x^2 + y^2 + z^2})}, \right.$$

$$\left(x \left(dx^2 x^2 \sqrt{x^2 + y^2 + z^2} + 2 dx dz x z \sqrt{x^2 + y^2 + z^2} + dz^2 z^2 \sqrt{x^2 + y^2 + z^2} + \right. \right.$$

$$\left. \left. 2 dx dz x z (-2 + 3 x^2 + 3 y^2 + 3 z^2) - dz^2 (2 (-1 + x^2 + y^2)(x^2 + y^2) + (x^2 + y^2) z^2 - z^4) + \right. \right.$$

$$\left. dt^2 (-1 + x^2 + y^2 + z^2) (-x^2 - y^2 - z^2 + \sqrt{x^2 + y^2 + z^2}) + 2 dy y (dx x + dz z) \right.$$

$$\left. \left(-2 + 3 x^2 + 3 y^2 + 3 z^2 + \sqrt{x^2 + y^2 + z^2} \right) + dx^2 (2 (y^2 + z^2) + (x^2 + y^2 + z^2) (x^2 - 2 (y^2 + z^2))) + \right.$$

$$\left. dy^2 (-2 x^4 + y^4 + 2 z^2 - 2 z^4 - x^2 (-2 + y^2 + 4 z^2) + y^2 (-z^2 + \sqrt{x^2 + y^2 + z^2})) \right) /$$

$$\left(2 (-1 + x^2 + y^2 + z^2) (x^2 + y^2 + z^2)^{5/2} \right), \left(y \left(dx^2 x^2 \sqrt{x^2 + y^2 + z^2} + 2 dx dz x z \sqrt{x^2 + y^2 + z^2} + \right. \right.$$

$$\left. dz^2 z^2 \sqrt{x^2 + y^2 + z^2} + 2 dx dz x z (-2 + 3 x^2 + 3 y^2 + 3 z^2) - \right.$$

$$\left. dz^2 (2 (-1 + x^2 + y^2)(x^2 + y^2) + (x^2 + y^2) z^2 - z^4) + dt^2 (-1 + x^2 + y^2 + z^2) (-x^2 - y^2 - z^2 + \sqrt{x^2 + y^2 + z^2}) + \right.$$

$$\left. 2 dy y (dx x + dz z) (-2 + 3 x^2 + 3 y^2 + 3 z^2 + \sqrt{x^2 + y^2 + z^2}) + \right.$$

$$\left. dx^2 (2 (y^2 + z^2) + (x^2 + y^2 + z^2) (x^2 - 2 (y^2 + z^2))) + \right.$$

$$\left. dy^2 (-2 x^4 + y^4 + 2 z^2 - 2 z^4 - x^2 (-2 + y^2 + 4 z^2) + y^2 (-z^2 + \sqrt{x^2 + y^2 + z^2})) \right) /$$

$$\left(2 (-1 + x^2 + y^2 + z^2) (x^2 + y^2 + z^2)^{5/2} \right),$$

$$\left(z \left(dx^2 x^2 \sqrt{x^2 + y^2 + z^2} + 2 dx dz x z \sqrt{x^2 + y^2 + z^2} + dz^2 z^2 \sqrt{x^2 + y^2 + z^2} + \right. \right.$$

$$\left. 2 dx dz x z (-2 + 3 x^2 + 3 y^2 + 3 z^2) - dz^2 (2 (-1 + x^2 + y^2)(x^2 + y^2) + (x^2 + y^2) z^2 - z^4) + \right.$$

$$\left. dt^2 (-1 + x^2 + y^2 + z^2) (-x^2 - y^2 - z^2 + \sqrt{x^2 + y^2 + z^2}) + 2 dy y (dx x + dz z) \right.$$

$$\left. \left(-2 + 3 x^2 + 3 y^2 + 3 z^2 + \sqrt{x^2 + y^2 + z^2} \right) + dx^2 (2 (y^2 + z^2) + (x^2 + y^2 + z^2) (x^2 - 2 (y^2 + z^2))) + \right.$$

$$\left. dy^2 (-2 x^4 + y^4 + 2 z^2 - 2 z^4 - x^2 (-2 + y^2 + 4 z^2) + y^2 (-z^2 + \sqrt{x^2 + y^2 + z^2})) \right) /$$

$$\left(2 (-1 + x^2 + y^2 + z^2) (x^2 + y^2 + z^2)^{5/2} \right) \left. \right\}$$

```
In[30]:= StringRiffle[{"double ddt = " <> ToString[CForm[equationsSimplified[[1]]] <> ";",
"double ddx = " <> ToString[CForm[equationsSimplified[[2]]] <> ";",
"double ddy = " <> ToString[CForm[equationsSimplified[[3]]] <> ";",
"double ddz = " <> ToString[CForm[equationsSimplified[[4]]] <> ";",
}, "\n\n"]
```

Out[30]=

```

double ddt = -((dt*(dx*x + dy*y + dz*z))/((Power(x,2) +
  Power(y,2) + Power(z,2))*(-1 + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))));

double ddx = (x*(Power(dx,2)*Power(x,2)*Sqrt(Power(x,2) + Power(y,2)
  + Power(z,2)) + 2*dx*dz*x*z*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) +
  Power(dz,2)*Power(z,2)*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*(-2
  + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2)) - Power(dz,2)*(2*(-1 + Power(x,2) +
  Power(y,2))*(Power(x,2) + Power(y,2)) + (Power(x,2) + Power(y,2))*Power(z,2) - Power(z,4))
  + Power(dt,2)*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*(-Power(x,2) - Power(y,2)
  - Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))) + 2*dy*y*(dx*x + dz*z)*(-2
  + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2) + Sqrt(Power(x,2) + Power(y,2) +
  Power(z,2))) + Power(dx,2)*(2*(Power(y,2) + Power(z,2)) + (Power(x,2) + Power(y,2) +
  Power(z,2))*(Power(x,2) - 2*(Power(y,2) + Power(z,2)))) + Power(dy,2)*(-2*Power(x,4) +
  Power(y,4) + 2*Power(z,2) - 2*Power(z,4) - Power(x,2)*(-2 + Power(y,2) + 4*Power(z,2))
  + Power(y,2)*(-Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2)))))/(2.*(-1 +
  Power(x,2) + Power(y,2) + Power(z,2))*Power(Power(x,2) + Power(y,2) + Power(z,2),2.5));

double ddy = (y*(Power(dx,2)*Power(x,2)*Sqrt(Power(x,2) + Power(y,2)
  + Power(z,2)) + 2*dx*dz*x*z*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) +
  Power(dz,2)*Power(z,2)*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*(-2
  + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2)) - Power(dz,2)*(2*(-1 + Power(x,2) +
  Power(y,2))*(Power(x,2) + Power(y,2)) + (Power(x,2) + Power(y,2))*Power(z,2) - Power(z,4))
  + Power(dt,2)*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*(-Power(x,2) - Power(y,2)
  - Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))) + 2*dy*y*(dx*x + dz*z)*(-2
  + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2) + Sqrt(Power(x,2) + Power(y,2) +
  Power(z,2))) + Power(dx,2)*(2*(Power(y,2) + Power(z,2)) + (Power(x,2) + Power(y,2) +
  Power(z,2))*(Power(x,2) - 2*(Power(y,2) + Power(z,2)))) + Power(dy,2)*(-2*Power(x,4) +
  Power(y,4) + 2*Power(z,2) - 2*Power(z,4) - Power(x,2)*(-2 + Power(y,2) + 4*Power(z,2))
  + Power(y,2)*(-Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2)))))/(2.*(-1 +
  Power(x,2) + Power(y,2) + Power(z,2))*Power(Power(x,2) + Power(y,2) + Power(z,2),2.5));

double ddz = (z*(Power(dx,2)*Power(x,2)*Sqrt(Power(x,2) + Power(y,2)
  + Power(z,2)) + 2*dx*dz*x*z*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) +
  Power(dz,2)*Power(z,2)*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*(-2
  + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2)) - Power(dz,2)*(2*(-1 + Power(x,2) +
  Power(y,2))*(Power(x,2) + Power(y,2)) + (Power(x,2) + Power(y,2))*Power(z,2) - Power(z,4))
  + Power(dt,2)*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*(-Power(x,2) - Power(y,2)
  - Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))) + 2*dy*y*(dx*x + dz*z)*(-2
  + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2) + Sqrt(Power(x,2) + Power(y,2) +
  Power(z,2))) + Power(dx,2)*(2*(Power(y,2) + Power(z,2)) + (Power(x,2) + Power(y,2) +
  Power(z,2))*(Power(x,2) - 2*(Power(y,2) + Power(z,2)))) + Power(dy,2)*(-2*Power(x,4) +
  Power(y,4) + 2*Power(z,2) - 2*Power(z,4) - Power(x,2)*(-2 + Power(y,2) + 4*Power(z,2))
  + Power(y,2)*(-Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2)))))/(2.*(-1 +
  Power(x,2) + Power(y,2) + Power(z,2))*Power(Power(x,2) + Power(y,2) + Power(z,2),2.5));

```

In[28]:= ToString[CForm[EquationsSimplified]]

Out[28]=

```
List(-((dt*(dx*x + dy*y + dz*z))/((Power(x,2) + Power(y,2) + Power(z,2))*(-1 + Sqrt(Power(x,2)
+ Power(y,2) + Power(z,2))))), (x*(Power(dx,2)*Power(x,2)*Sqrt(Power(x,2) + Power(y,2)
+ Power(z,2)) + 2*dx*dz*x*z*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) +
Power(dz,2)*Power(z,2)*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*(-2
+ 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2)) - Power(dz,2)*(2*(-1 + Power(x,2)
+ Power(y,2))*(Power(x,2) + Power(y,2)) + (Power(x,2) + Power(y,2))*Power(z,2) -
Power(z,4)) + Power(dt,2)*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*(-Power(x,2) -
Power(y,2) - Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))) + 2*dy*y*(dx*x +
dz*z)*(-2 + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2) + Sqrt(Power(x,2) + Power(y,2)
+ Power(z,2))) + Power(dx,2)*(2*(Power(y,2) + Power(z,2)) + (Power(x,2) + Power(y,2)
+ Power(z,2))*(Power(x,2) - 2*(Power(y,2) + Power(z,2)))) + Power(dy,2)*(-2*Power(x,4)
+ Power(y,4) + 2*Power(z,2) - 2*Power(z,4) - Power(x,2)*(-2 + Power(y,2)
+ 4*Power(z,2)) + Power(y,2)*(-Power(z,2) + Sqrt(Power(x,2) + Power(y,2) +
Power(z,2)))))/(2.*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*Power(Power(x,2)
+ Power(y,2) + Power(z,2),2.5)), (y*(Power(dx,2)*Power(x,2)*Sqrt(Power(x,2) +
Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) +
Power(dz,2)*Power(z,2)*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*(-2
+ 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2)) - Power(dz,2)*(2*(-1 + Power(x,2)
+ Power(y,2))*(Power(x,2) + Power(y,2)) + (Power(x,2) + Power(y,2))*Power(z,2) -
Power(z,4)) + Power(dt,2)*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*(-Power(x,2) -
Power(y,2) - Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))) + 2*dy*y*(dx*x +
dz*z)*(-2 + 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2) + Sqrt(Power(x,2) + Power(y,2)
+ Power(z,2))) + Power(dx,2)*(2*(Power(y,2) + Power(z,2)) + (Power(x,2) + Power(y,2)
+ Power(z,2))*(Power(x,2) - 2*(Power(y,2) + Power(z,2)))) + Power(dy,2)*(-2*Power(x,4)
+ Power(y,4) + 2*Power(z,2) - 2*Power(z,4) - Power(x,2)*(-2 + Power(y,2)
+ 4*Power(z,2)) + Power(y,2)*(-Power(z,2) + Sqrt(Power(x,2) + Power(y,2) +
Power(z,2)))))/(2.*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*Power(Power(x,2)
+ Power(y,2) + Power(z,2),2.5)), (z*(Power(dx,2)*Power(x,2)*Sqrt(Power(x,2) +
Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) +
Power(dz,2)*Power(z,2)*Sqrt(Power(x,2) + Power(y,2) + Power(z,2)) + 2*dx*dz*x*z*(-2
+ 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2)) - Power(dz,2)*(2*(-1 + Power(x,2)
+ Power(y,2))*(Power(x,2) + Power(y,2)) + (Power(x,2) + Power(y,2))*Power(z,2) - Power(z,4))
+ Power(dt,2)*(-1 + Power(x,2) + Power(y,2) + Power(z,2))*(-Power(x,2) - Power(y,2)
- Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2))) + 2*dy*y*(dx*x + dz*z)*(-2
+ 3*Power(x,2) + 3*Power(y,2) + 3*Power(z,2) + Sqrt(Power(x,2) + Power(y,2) +
Power(z,2))) + Power(dx,2)*(2*(Power(y,2) + Power(z,2)) + (Power(x,2) + Power(y,2) +
Power(z,2))*(Power(x,2) - 2*(Power(y,2) + Power(z,2)))) + Power(dy,2)*(-2*Power(x,4)
+ Power(y,4) + 2*Power(z,2) - 2*Power(z,4) - Power(x,2)*(-2 + Power(y,2) + 4*Power(z,2))
+ Power(y,2)*(-Power(z,2) + Sqrt(Power(x,2) + Power(y,2) + Power(z,2)))))/(2.*(-1 +
Power(x,2) + Power(y,2) + Power(z,2))*Power(Power(x,2) + Power(y,2) + Power(z,2),2.5)))
```

NB: you can use code like this to generate simpler representations where multiplication is used instead of “power”.

```
parser = StringReplace[ToString[CForm[#]], Shortest["Power(" ~~ x_ ~~ ",2)"] → x <> "*" <> x] &;
```